T. S. Khasanshin and T. B. Zykova

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Analytical expressions are obtained for the temperature dependence of the isobaric specific heat of liquid methanol and the $\mathrm{C}_{11}-\mathrm{C}_{18} \mathrm{~N}$-alcohols at 293-583 K at atmospheric pressure.

It is well known that experimental determination of specific heat is beset with significant technological difficulties. In connection with this, it is important to consider computation methods for determining thermodynamic properties, one of which is based on use of the law of change in properties in homological series. Use of this method permits, first, interrelationship of properties of various materials within a homological series, and second, interpolation or, within reason, extrapolation to determine such properties for members of the series for which they are unknown. A similar approach was used earlier [1] to find density in the N -alcohol series.

The goal of the present study is to investigate behavior of isobaric specific heat at atmospheric pressure in the series of pure liquid saturated monatomic alcohols.

The specific heat $C p$ of these alcohols has not been sufficiently studied experimentally. The lower alcohols up to pentanol-1 have been studied most thoroughly, the higher ones, less so. The handbook [2] contains citations of experimental data on $C p$ of the alcohols with $C_{1}-C_{15}, C_{18}$. It should be noted that this same handbook considers practically all the more reliable experimental data existing for $C p$ of alcohols with normal structure. For the alcohols with $C_{16}, C_{17}$, and those with a number of carbon atoms ( $N$ ) greater than 18 information on Cp is practically absent from the literature.

The uncertainty of the measurements at at atmospheric pressure for the alcohols $C_{1}-C_{5}$ does not exceed $0.3 \%$, with the exception of butanol-1, for which it comprises approximately $1 \%$ for $T>322 \mathrm{~K}$. The specific heat of the higher alcohols ( $\mathrm{C}_{6}-\mathrm{C}_{15}, \mathrm{C}_{18}$ ) has been measured with an uncertainty of the order of $1.0-2.5 \%$.

An analytical generalization generalization of experimental data on Cp for the alcohols $C_{2}-C_{8}, C_{10}$ in the temperature range from the normal fusion point to the boiling point was performed in [1, 3-9]. The accuracy of the approximation oscillated depending on the temperature interval and number of the homolog, but lay in the limits $0.1-2.0 \%$.

Preliminary processing of the available information was carried out in the coordinates $\mathrm{Cp}, \mathrm{N}$ by graphing experimental points [2] for the alcohols $\mathrm{C}_{7}-\mathrm{C}_{15}, \mathrm{C}_{18}$ and generalization results $[1,3-9]$ for the alcohols $C_{3}-C_{8}, C_{10}$ taken at identical temperatues in the range 293583 K in 10 K steps. This construction revealed that the original CP data fitted a series of curves (isotherms) with a scattering not exceeding $\pm 0.2, \pm 0.5,0.7 \%$ for $C_{3}, C_{4}$, $C_{5}$, and $\pm 1.2 \%$ for $C_{6}-C_{11}, C_{13}, C_{14}, C_{18}$. For the $C_{12}$ and $C_{15}$ alcohols the deviations lie in the range $2-4 \%$ and are of a systemic character (positive for $C_{12}$ ). Thus, the processing results indicate that in the normal alcohol series within the limits of the estimated uncertainties (1.0-2.5\%) the initial data show a dependence of specific heat on number of carbon atoms in the alcohol molecule at constant temperature. Analysis of this dependence revealed that the curves are continuously decreasing curves convex in the direction of the $N$-axis. Analytical smoothing of the original data in the coordinates $C p, N$ was accomplished by power series. The internal consistency of $C p$ values calculated in this manner was tested by constructing atmospheric pressure isobars in the coordinates Cp , T . This is of special importance, since the function $C p=f(T)$ for these alcohols is of a compplex character. The scattering of values (taken at identical temperatues) relative to the smoothed curves for both graphs did not exceed $0.3 \%$.

[^0]TABLE 1. Coefficients of Eq. (1)

| Alcohol | $a_{0}$ | $a_{1}$ | $a_{2}$ | $a_{3}$ | $a_{4}$ | $a_{5}$ | Temp. <br> interval <br> K |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Methanol | 2,786 | $-5,1901$ | 5,7584 | 29,471 | - | - | 176-337 |
| Undecanol-1 | 33,376 | -413,191 | 2039, 87 | -4725,27 | 5221,61 | -2216,94 | 293-513 |
| Dodecanol-1 | 43,274 | $-534,623$ | 2635,80 | -6187,30 | 7010,79 | -3089,73 | 303-533 |
| Tridecanol-1 | 44,356 | -546,727 | 2690,30 | -6310,15 | 7145,50 | -3145,80 | 313-553 |
| Tetradecanol-1 | 26,370 | -340,010 | 1747,54 | -4176,73 | 4746,21 | -2071,69 | 313-563 |
| Pentadecanol-1 | 42,001 | -526,527 | 2631,01 | $-6252,82$ | 7163,85 | -3187,22 | 323-583 |
| Hexadecanol-1 | 22,396 | - 313,331 | 1714,97 | $-4308,90$ | 5124,66 | $-2340,56$ | 333-583 |
| Heptadecanol-1 | $-24,176$ | 206,491 | $-582,30$ | 717,10 | $-322,25$ | - | 333-583 |
| Octadecanol-1 | -48,906 | 472,034 | $-1711,57$ | 3094,86 | -2802,55 | 1025,83 | 343-583 |

TABLE 2. Isobaric Specific Heat of Liquid Methanol at Atmospheric Pressure

| $T, \mathrm{~K}$ | $C \mathrm{C}, \mathrm{k}, \mathrm{K})$ <br> $\mathrm{kJ} /(\mathrm{kg})$ | $\mathrm{T}, \mathrm{K}$ | Cp, <br> $\mathrm{kJ} / \mathrm{kg} \cdot \mathrm{K})$ |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
| 175,49 | 2,2118 | 258,15 | 2,3369 |
| 178,15 | 2,2108 | 263,15 | 2,3560 |
| 183,15 | 2,2096 | 268,15 | 2,3766 |
| 188,15 | 2,2096 | 273,15 | 2,3986 |
| 193,15 | 2,2107 | 278,15 | 2,4221 |
| 198,15 | 2,2130 | 283,15 | 2,4471 |
| 203,15 | 2,2164 | 288,15 | 2,4737 |
| 208,15 | 2,2210 | 293,15 | 2,5018 |
| 213,15 | 2,2267 | 298,15 | 2,5315 |
| 218,15 | 2,2338 | 303,15 | 2,5629 |
| 223,15 | 2,2421 | 308,15 | 2,5958 |
| 228,15 | 2,2516 | 313,15 | 2,6304 |
| 233,15 | 2,2625 | 318,15 | 2,6667 |
| 238,15 | 2,2746 | 323,15 | 2,7047 |
| 243,15 | 2,2881 | 328,15 | 2,7443 |
| 248,15 | 2,3030 | 333,15 | 2,7858 |
| 253,15 | 2,3193 | 337,70 | 2,8250 |

TABLE 3. Isobaric Specific Heat (kJ/(kg.K)) of Liquid Alcohols at Atmospheric Pressure

| $T, \mathrm{~K}$ | $\mathrm{C}_{11}$ | $\mathrm{C}_{12}$ | $\mathrm{C}_{13}$ | $\mathrm{C}_{14}$ | $\mathrm{C}_{15}$ | $\mathrm{C}_{1}$ | $\mathrm{C}_{17}$ | $\mathrm{C}_{18}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 293, 15 | 2,271 |  | - | - | - | - | - |  |
| 303, 15 | 2,361 | 2,358 | - | - | - | - |  |  |
| 313, 15 | 2,452 | 2,443 | 2,433 | 2,407 | - | - | - |  |
| 323, 15 | 2,542 | 2,528 | 2,515 | 2,495 | 2,484 |  |  |  |
| 333, 15 | 2,627 | 2,610 | 2,596 | 2,579 | 2,565 | 2,550 | 2,533 |  |
| 343, 15 | 2,708 | 2,688 | 2,672 | 2,656 | 2,640 | 2,629 | 2,622 | 2,607 |
| 353, 15 | 2,783 | 2,761 | 2,742 | 2,726 | 2,708 | 2,700 | 2,696 | 2,686 |
| 363, 15 | 2,851 | 2,827 | 2,806 | 2,788 | 2,769 | 2,761 | 2,757 | 2,750 |
| 373, 15 | 2,911 | 2,885 | 2,862 | 2,843 | 2,823 | 2,814 | 2,807 | 2,800 |
| 383, 15 | 2,963 | 2,935 | 2,911 | 2,889 | 2,868 | 2,857 | 2,848 | 2,840 |
| 393, 15 | 3,007 | 2,978 | 2,952 | 2,928 | 2,906 | 2,893 | 2,879 | 2,870 |
| 403, 15 | 3,044 | 3,013 | 2,985 | 2,960 | 2,937 | 2,921 | 2,904 | 2,893 |
| 413, 15 | 3,074 | 3,042 | 3,012 | 2,985 | 2,960 | 2,943 | 2,923 | 2,910 |
| 423, 15 | 3,097 | 3,063 | 3,032 | 3,004 | 2,978 | 2,959 | 2,938 | 2,923 |
| 433,15 | 3,114 | 3,080 | 3,048 | 3,018 | 2,991 | 2,971 | 2,948 | 2,932 |
| 443, 15 | 3,127 | 3,092 | 3,058 | 3,029 | 2,999 | 2,979 | 2,956 | 2,939 |
| 453, 15 | 3,136 | 3,100 | 3,065 | 3,036 | 3,005 | 2,985 | 2,963 | 2,945 |
| 463,15 | 3,142 | 3,105 | 3,070 | 3,040 | 3,009 | 2,989 | 2,968 | 2,950 |
| 473, 15 | 3,147 | 3, 109 | 3,074 | 3,044 | 3,013 | 2,993 | 2,973 | 2,955 |
| 483, 15 | 3,151 | 3,113 | 3,078 | 3,048 | 3,017 | 2,998 | 2,979 | 2,961 |
| 493, 15 | 3,156 | 3,117 | 3,082 | 3,052 | 3,022 | 3,004 | 2,986 | 2,968 |
| 503, 15 | 3,163 | 3,122 | 3,088 | 3,059 | 3,029 | 3,012 | 2,994 | 2,977 |
| 513,15 | 3,173 | 3,129 | 3,097 | 3,068 | 3,039 | 3,023 | 3,005 | 2,987 |
| 523,15 | - | 3,139 | 3,108 | 3,080 | 3,053 | 3,037 | 3,018 | 3,000 |
| 533, 15 | - | 3,152 | 3,123 | 3,097 | 3,070 | 3,055 | 3,034 | 3,016 |
| 543, 15 | - | - | 3,141 | 3,118 | 3,091 | 3,075 | 3,053 | 3,034 |
| 553, 15 | - | - | 3,162 | 3,143 | 3,115 | 3,098 | 3,075 | 3,055 |
| $563,15$ | - | - | - | 3,174 | 3,141 | 3,124 | 3,101 | 3,079 |
| $573,15$ | - | - | - | - | 3,169 | 3,151 | 3,129 | 3,106 |
| 583,15 | - | - | - | - | 3,196 | 3,178 | 3,161 | 3,137 |

Finally, the smoothed $C p$ values of the $C_{11}-C_{18}$ alcohols were described by equations of the form

$$
\begin{equation*}
C_{p}=\sum_{i=0}^{n} a_{i}(T / 1000)^{i}, \tag{2}
\end{equation*}
$$

where $C_{p}$ is the isobaric specific heat, $\mathrm{kJ} /(\mathrm{kg} \cdot \mathrm{K}), \mathrm{T}$ is temperature, K .
The coefficients of Eq. (1) were calculated by the method of least squares and are presented in Table 1. Also shown for each alcohol is the temperature range used.

Since methanol, the first member of the series, lies outside the observation range (as does ethanol) so that the literature has no reliable information on Cp , a separate equation of the form of Eq. (1) was constructed for that substance using the most reliable experimental data of [11] and [12], obtained at temperatures of 313-383 and 180-320 K using the coefficients $a_{i}$ presented in Table 1. The specific heat values of [11], essentially determined in the liquid phase along the saturation curve were recalculated to atmospheric pressure for $T \leq 337.70 \mathrm{~K}$. The value of the correction was less than $0.1 \%$.

The possible error of the recommended Cp values (Tables 2 and 3) calculated with Eqs. (1) with the coefficients presented in Table 1 for methanol for the temperature range from the fusion point ( $\mathrm{T}=175.49 \mathrm{~K}$ [10]) to the boiling point ( $\mathrm{T}=337.70 \mathrm{~K}$ ) is in the range $0.1-$ $0.3 \%$ while the corresponding value for the $\mathrm{C}_{11}-\mathrm{C}_{18}$ alcohols is approximately $2.5 \%$.

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